# Honors Algebra II Notes Section 4.7 <br> Write and Apply Exponential and Power Functions 

Example 1 Write an exponential function $y=a b^{x}$ whose graph passes through (1, 12) and (3, 108).

## STEPS

1. Substitute both points into exponential function
2. Solve for a in the 1st equation, substitute the result into the 2nd equation
3. Substitute $a \varepsilon b$ into $y=a b x$

TRANSFORMING EXPONENTIAL DATA: a set of more than 2 points fits an exponential pattern if and only if the set of transformed points ( $x, \ln y$ ) fits a linear pattern.

Graph of points ( $x, y$ )


The graph is an exponential curve.

Graph of points $(x, \ln y)$


The graph is a line.

| Example 2 |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| x | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| y | 12 | 16 | 25 | 36 | 50 | 67 | 96 |

STEPS

1. Draw a scatter plot of the data ( $x$, In $y$ ).

Is an exponential model a good fit?

| $x$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ |  |  |  |  |  |  |  |

2. Plot the points

3. Find an exponential model $y=a b x$.
**choose 2 points on the line to find the slope**
**Use the point slope formula to find the model

## Example 3 Repeat Example 2 using a graphing calculator. Predict y if $x=8$.

## STEPS

1. Enter date into List 1 and List 2
2. Perform an exponential regression
3. Substitute $x=8$ into the exponential function

Power Function: $\quad \mathbf{y}=\boldsymbol{a} \boldsymbol{x}^{\boldsymbol{b}}$

## Example 4 Write a power function $y=a x^{b}$ whose graph passes through $(3,2)$

 and ( 6,9 ).STEPS

1. Substitute both points into power function
2. Solve for a in the ist equation, substitute the result into the $2 n d$ equation
3. Substitute $a \varepsilon b$ into $y=a x^{b}$

TRANSFORMING POWER DATA: a set of more than 2 points fits an power pattern if and only if the set of transformed points $(\ln x, \ln y)$ fits a linear pattern.


Graph of points $(\ln x, \ln y)$


The graph is a line.

Example 5

| x | 1.9 | 2.92 | 3.41 | 5.35 | 840 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| y | 0.23 | 1.04 | 1.69 | 6.76 | 16.03 |

## STEPS

1. Draw a scatter plot of the data $(\operatorname{In} x, \ln y)$.

Is a power model a good fit?

2. Plot the points
3. Find an exponential model $y=a x^{b}$.

**choose 2 points on the line to find the slope** **Use the point slope formula to find the model

## Example 3 Repeat Example 5 using a graphing calculator. Predict $y$ if $x=4.5$

## STEPS

1. Enter date into List 1 and List 2
2. Perform a power regression
3. Substitute $x=4.5$ into the power function $\qquad$
